

# Theory of the optical properties of segregated (InAs)/(GaSb) superlattices

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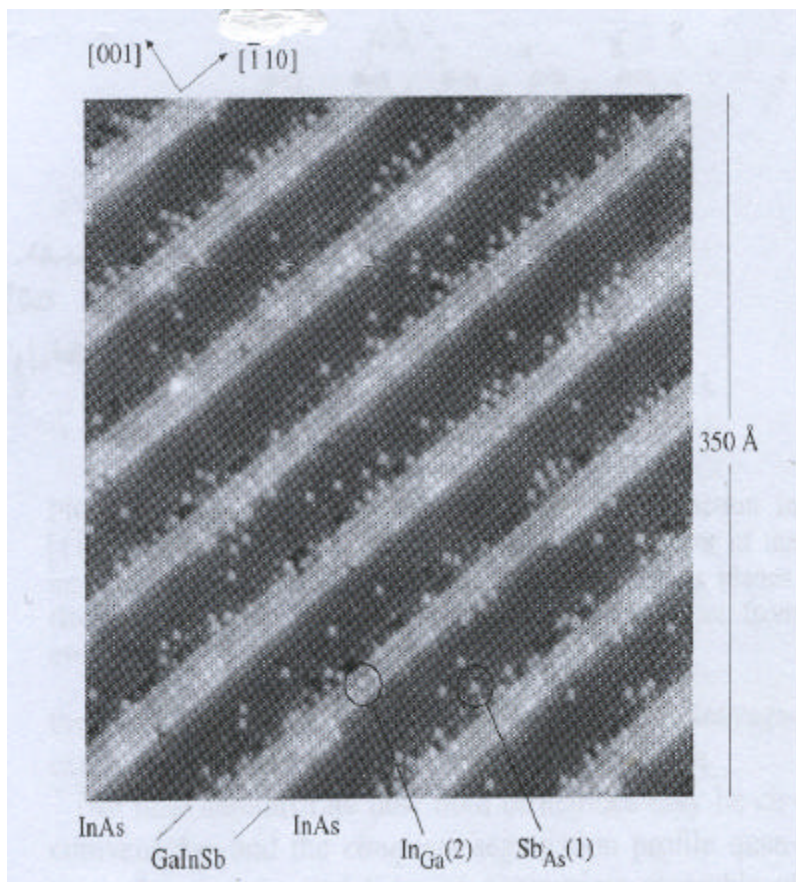
- Alex Zunger

*NREL, Golden, Colorado  
USA*

# Why to study segregation and interfacial disorder effects?

(for example on the optical spectra)

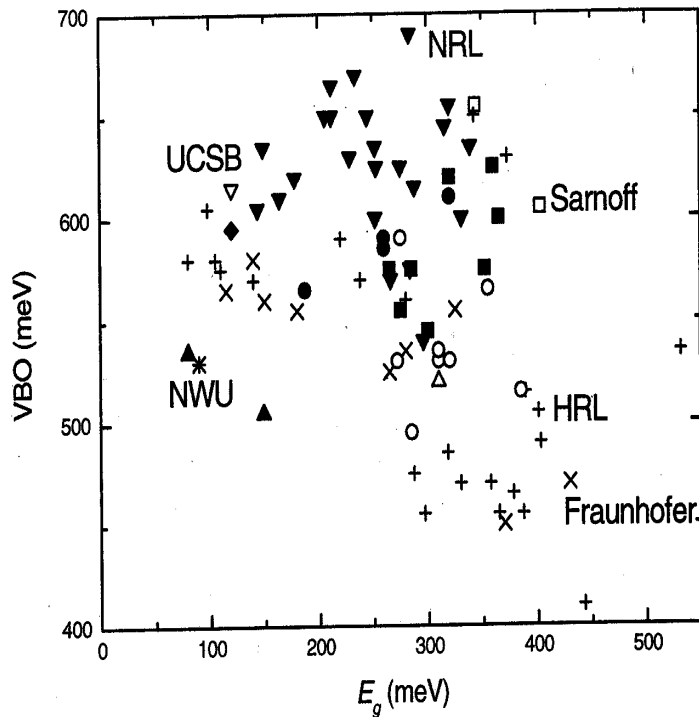
- First Reason: because some deviations from interfacial abruptness are always present in real samples.



(Steinshnider et al. PRL  
85,4562 (2000))

- Sb within InAs
- As and In within GaSb
- Interfacial broadening
- Normal (InAs-on-GaSb) IF rougher and more intermixed than inverted IF (Feenstra et al. PRL 72,2749 (1994))
- GaAs-like IF rougher than InSb-like IF (Twigg et al. Philos. Mag. 7,7,(1998))

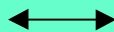
# Possible effects on the gaps of InAs/GaSb SLs and MQWs



- Vurgaftman et al. JAP 89,5815 (2001) fit the measured gaps to 8-band  $\mathbf{k}\cdot\mathbf{p}$  theory to extract an average VBO for InAs/GaSb.

- Differences between average offsets derived using data from different groups
- Differences as large as 100 meV for structures that are nominally similar!

Different  
microscopic  
morphology  
(for nominally  
identical structures)



Conspicuous  
differences in gaps

# Our EPM

- **SL Symmetry Effects**

Atomistic approach - we fully solve the single-particle Schrödinger equation where the SL potential is the sum of the atomic screened potentials. This takes into account fully the ( $D_{2d}$  or  $C_{2v}$ ) SL symmetry.

$$V(\underline{r}) = \sum_{na} v_a(|\underline{r} - \underline{R}_{na}|)$$

where

$$v_a(|\underline{r} - \underline{R}_{na}|) = \sum_q e^{iq \cdot (\underline{r} - \underline{R}_{na})} v_a(|q|) [1 + \mathbf{d}v]$$

and

$$v_a(|q|) = a_0^a \frac{q^2 - a_1^a}{a_2^a e^{a_3^a q^2} - 1}$$

is a continuous function of  $q$

- **Environmental Effects**

Appropriate potentials for the interface bonds In-Sb and Ga-As

We fit the EPM to:

- experimental gaps
- exptl effective masses
- exptl hydrostatic and biaxial deformation potentials
- LDA-predicted single band edge deformation potentials
- band offsets

of ALL the binary compounds: GaSb, InAs, GaAs and InSb.

Atomic pseudopotentials of Ga in GaSb and in GaAs are different

The potential on each atom is specific of its n.n. environment

$$v_{\text{In}}(\text{As}_n\text{Sb}_{4-n}) = \frac{n}{4} v_{\text{In}}(\text{InAs}) + \frac{4-n}{n} v_{\text{In}}(\text{InSb})$$

- **Strain Effects**

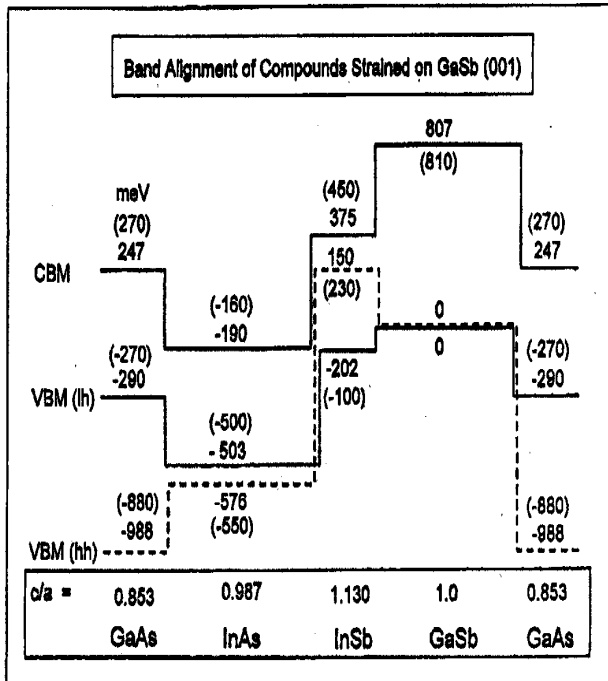
Our EPM include a parameter fit to the gap and band edge deformation potentials.

$$d v_{n a}(\mathbf{e}) = a_4^a \text{Tr}(\mathbf{e})$$

Atomic positions  $R_{n a}$  in the crystal are locally displaced by a VFF approach

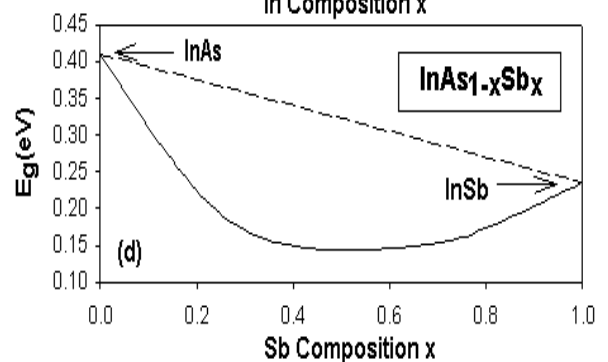
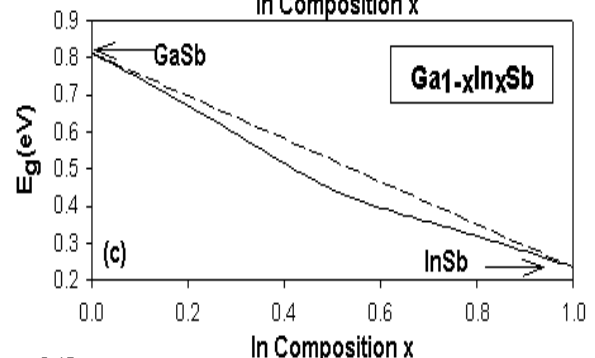
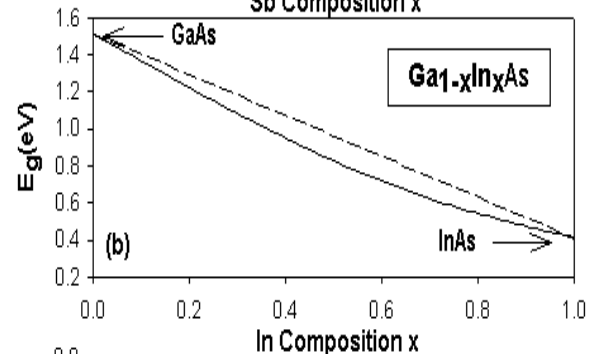
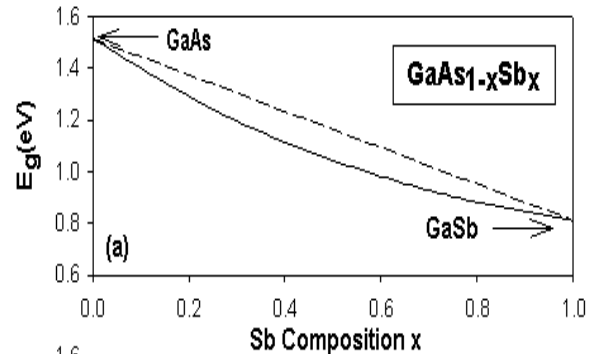
# Capabilities of the EPM

## IF specific offsets



To describe

- IF wavefunction localization
- alloying effects at IF

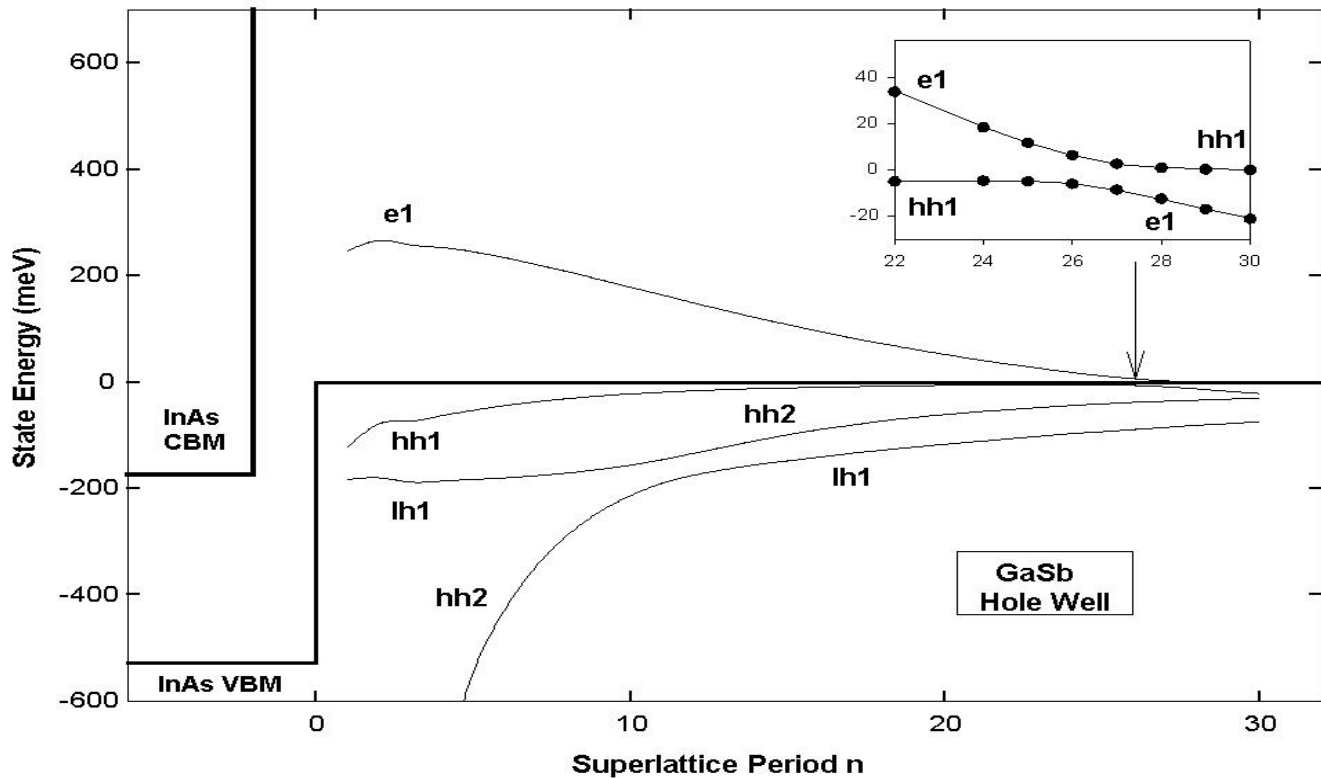


Gap bowing parameters of ternary alloys

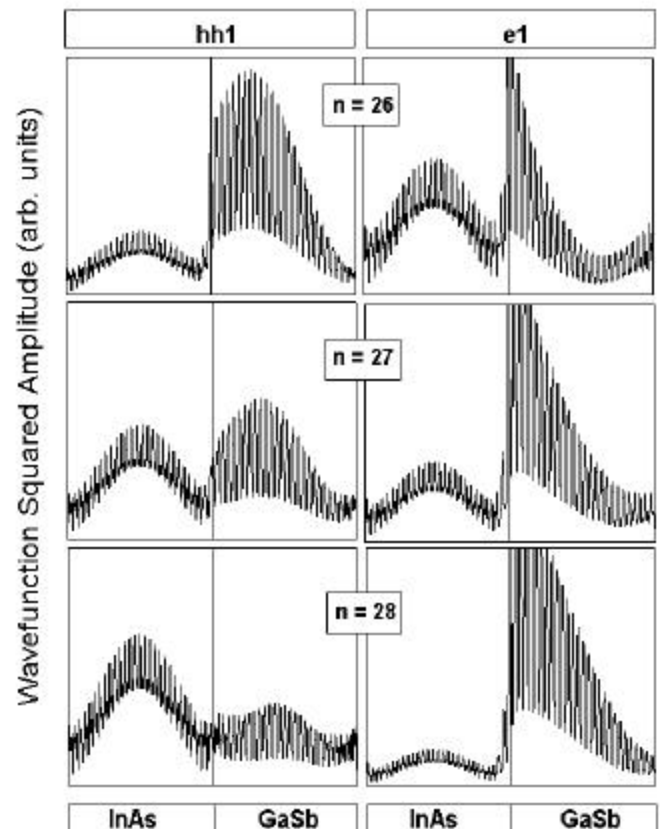
**Brief summary of the  
results for the abrupt  
superlattices**



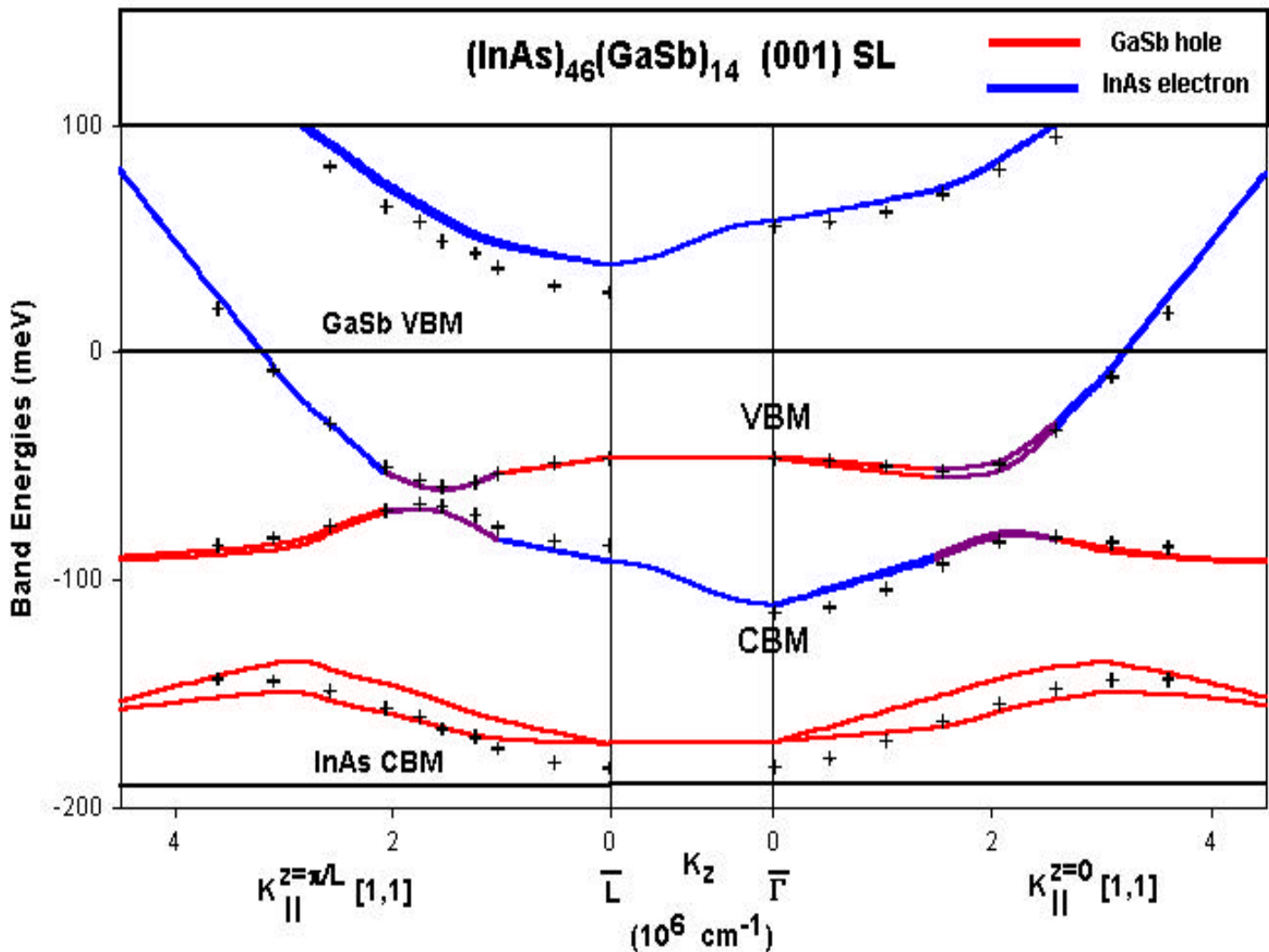
# Abrupt $(\text{InAs})_n / (\text{GaSb})_n$ SLs



- Anticrossing period in agreement with experiment



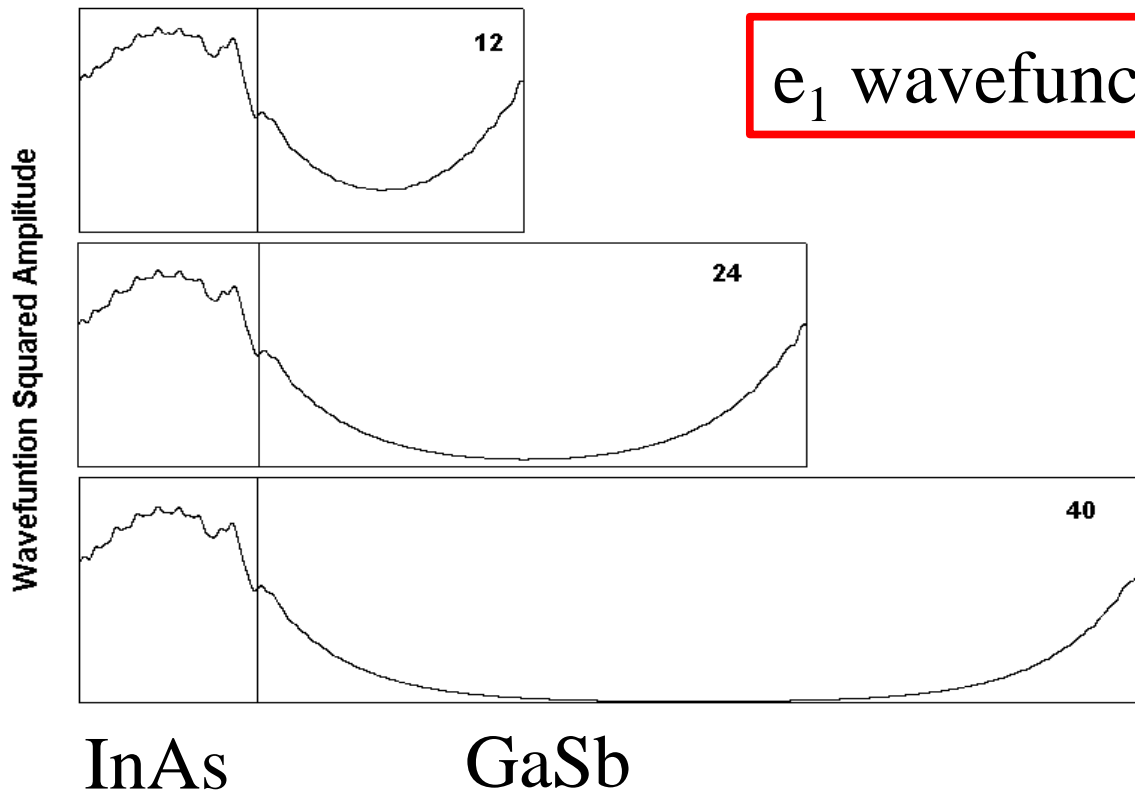
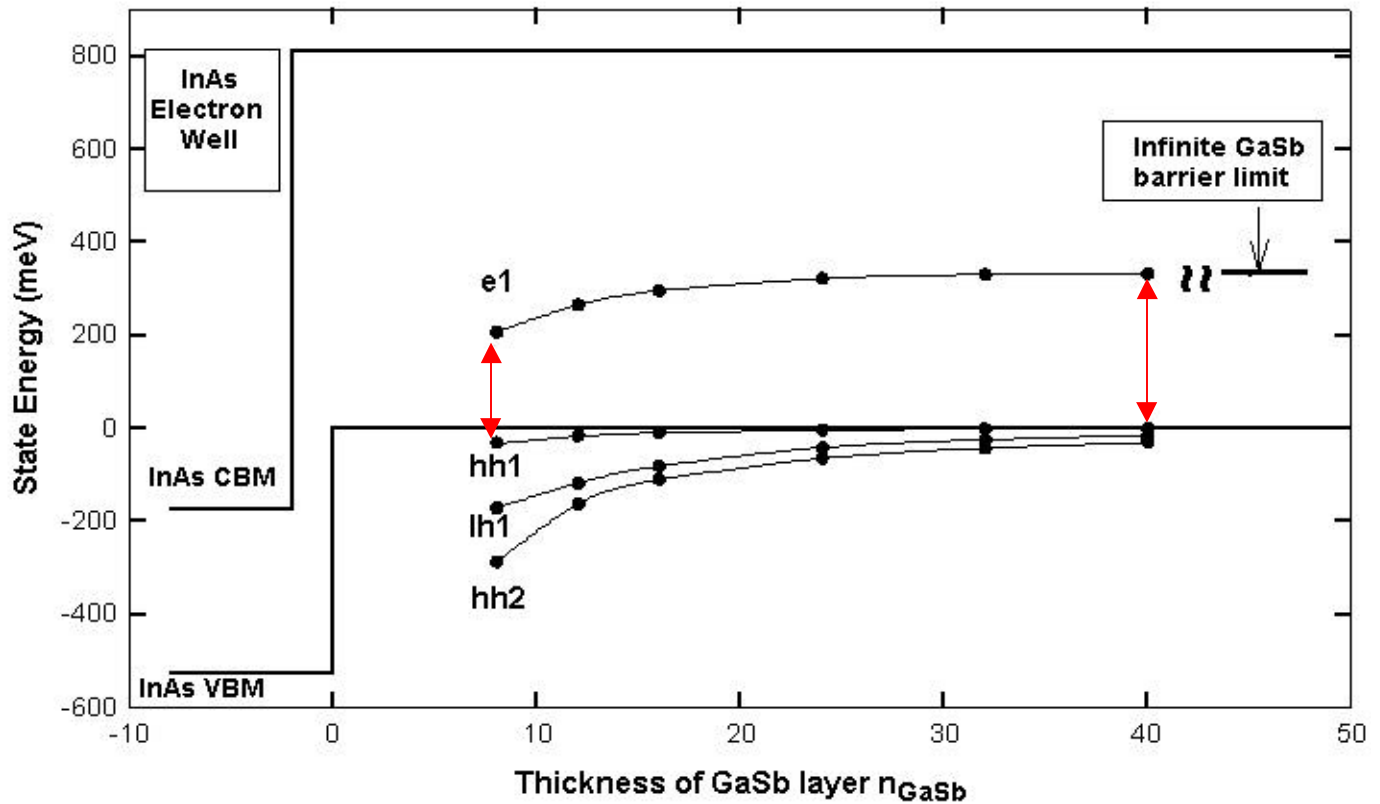
# Anticrossing semiconducting band gap



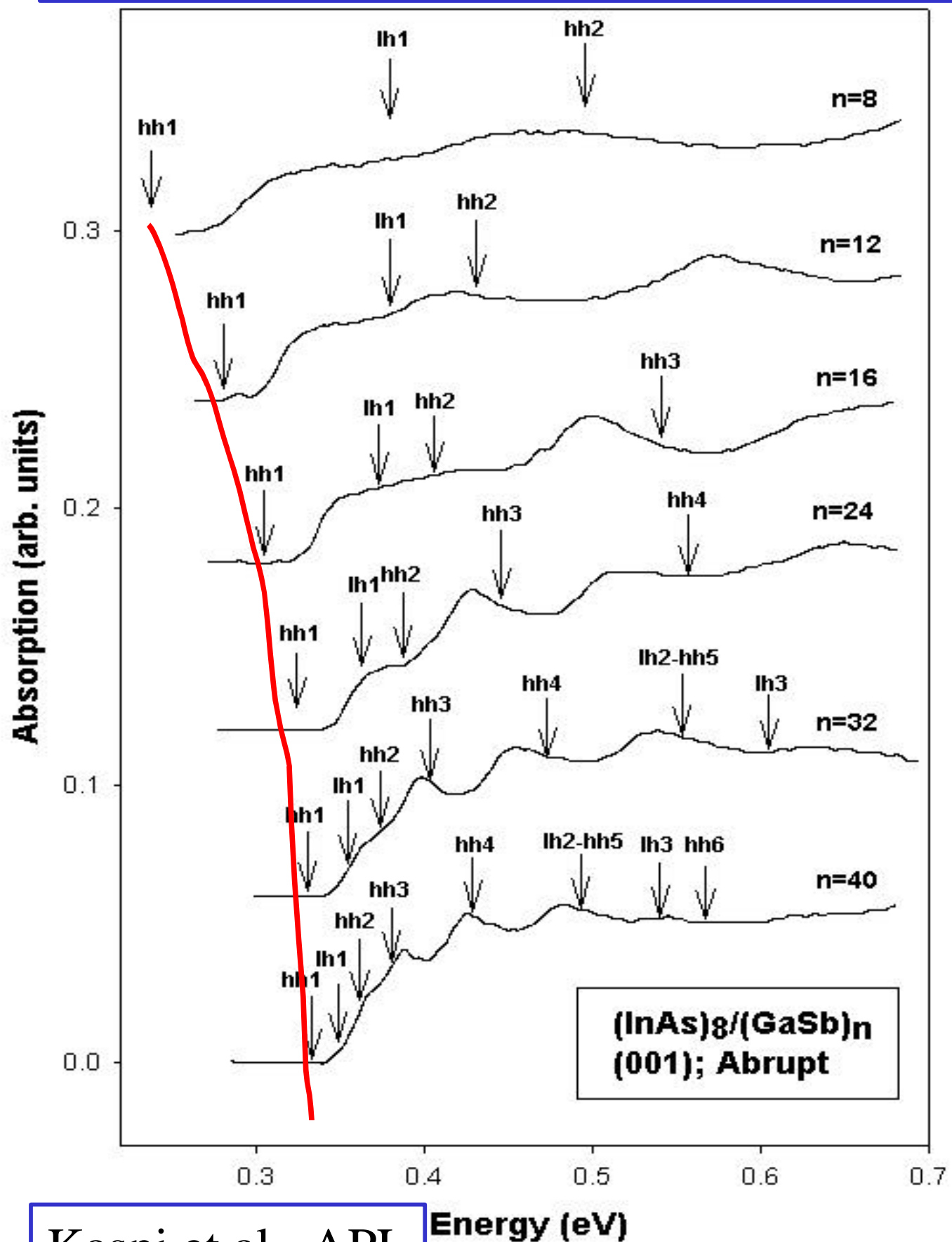
Smaller gap 2-8 meV

- Magri et al., PRB 61,10235 (2000)

# Abrupt $(\text{InAs})_8 / (\text{GaSb})_n$ SL's



- Arrows - calculated transition energies



Kaspi et al., APL  
76, 409 (2000)

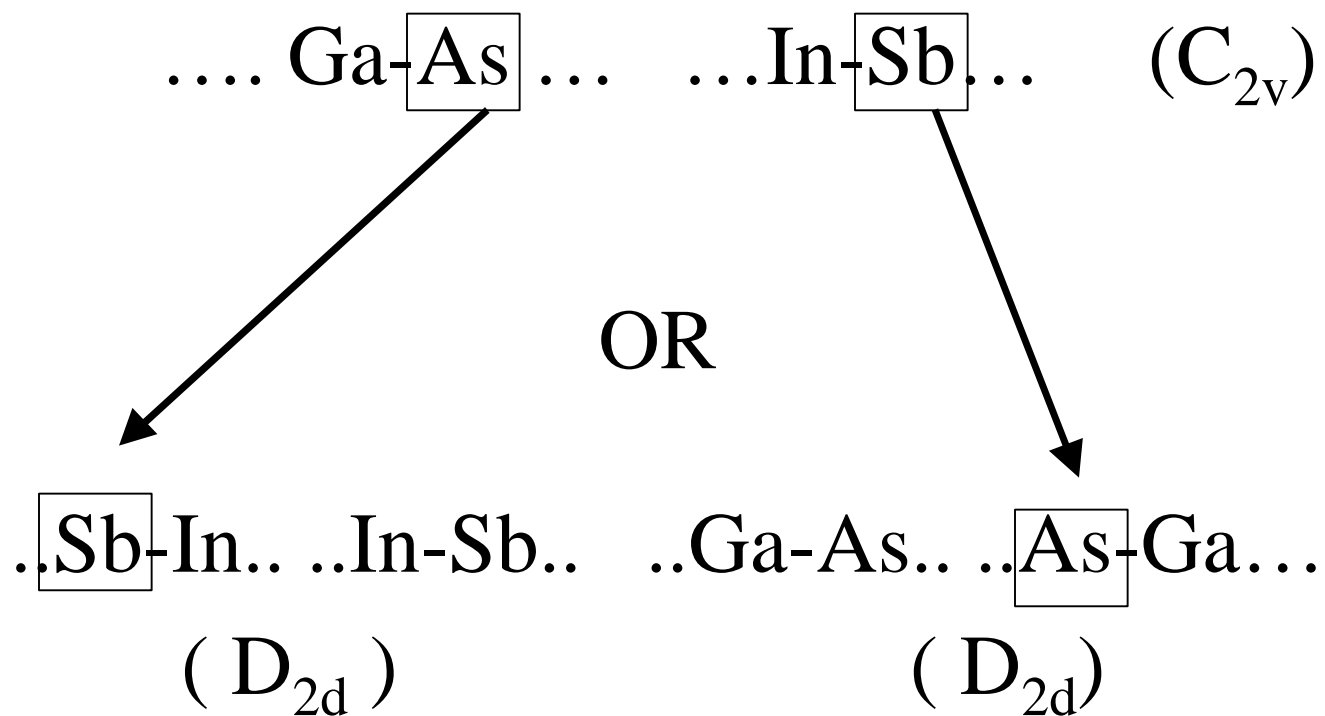
# Interface Interdiffusion Models

We consider two models:

- **Model I:** The Single-Layer Disorder Model  
(to study the effect of the *nature* of the interfacial bonds)
- **Model II:** The Kinetic Model of MBE growth  
(to study the effect of atomic segregation)

# Model I: the single-layer model of interfacial disorder

We start from:

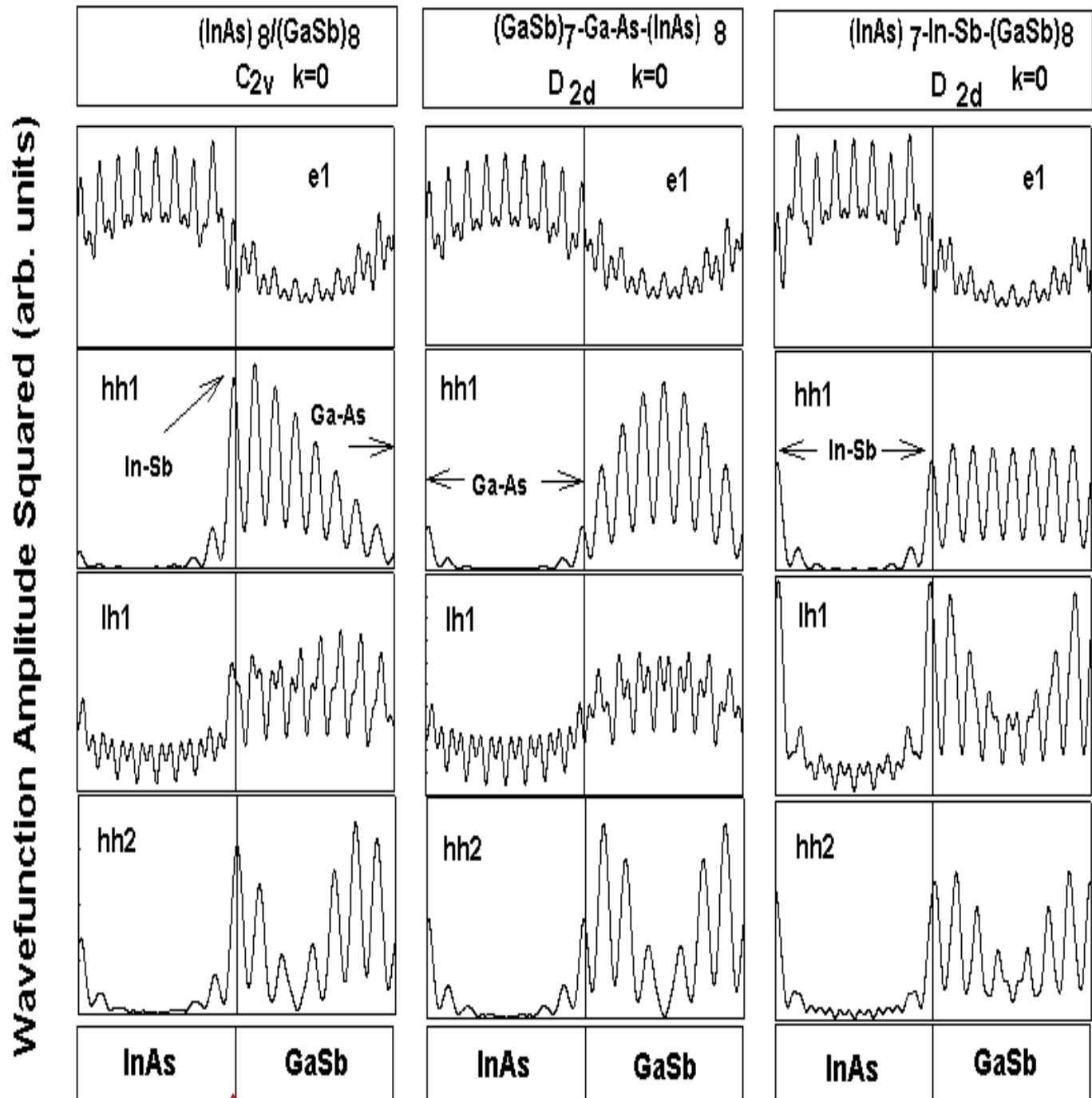


the composition of the interface anion plane is  
changed CONTINUOUSLY

What happens to the electronic  
structure?

# Model I

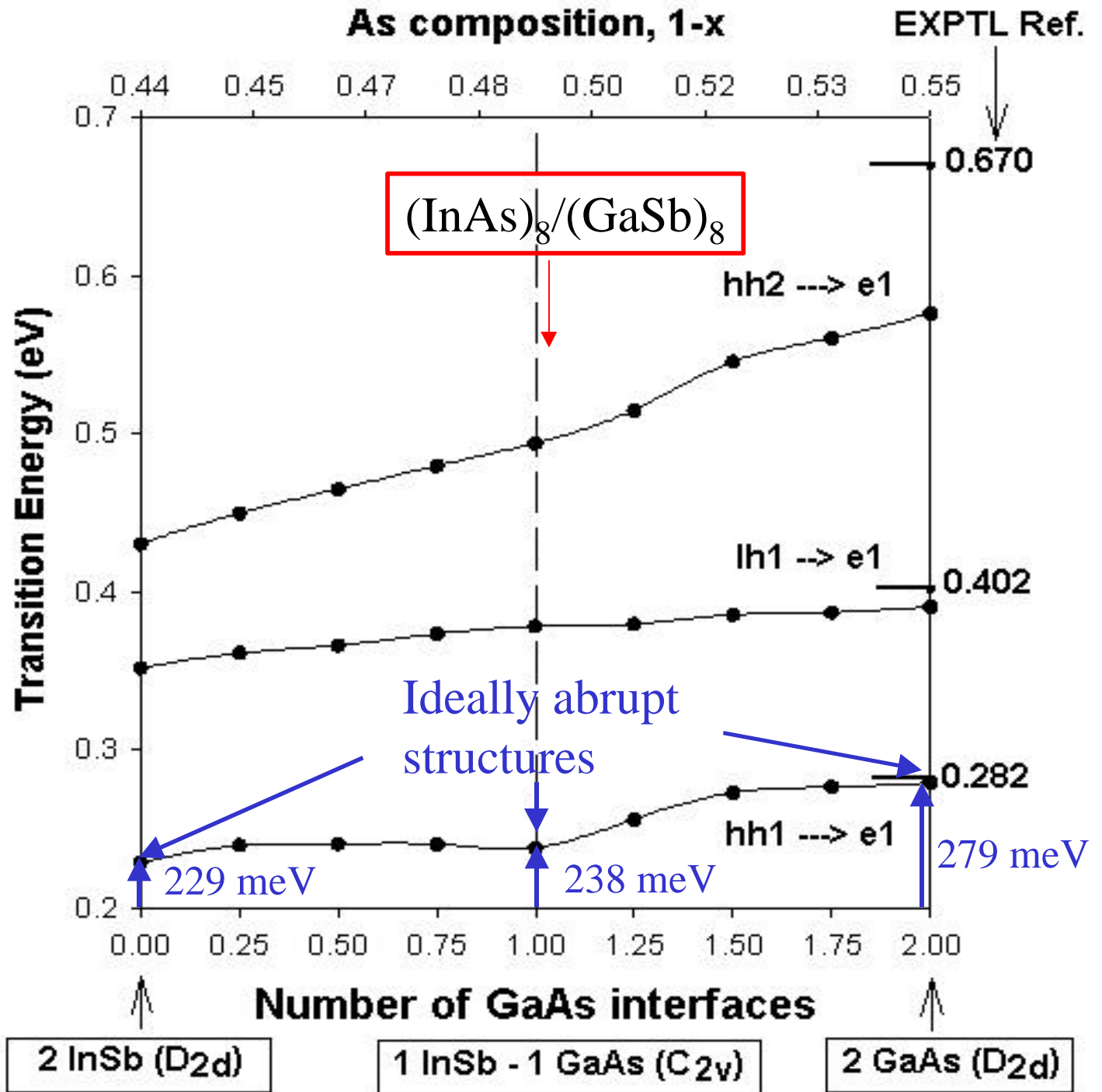
## Electron and hole wavefunctions



In-Sb IF

- Strong heavy hole localization on In-Sb IF

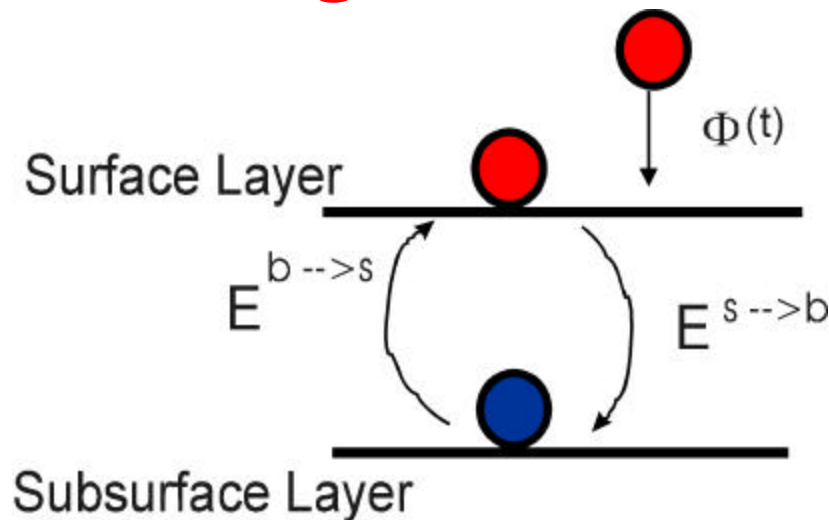
# Interband transition energies



- Gap 50 meV higher for Ga-As interfacial bonds than for In-Sb IF bonds



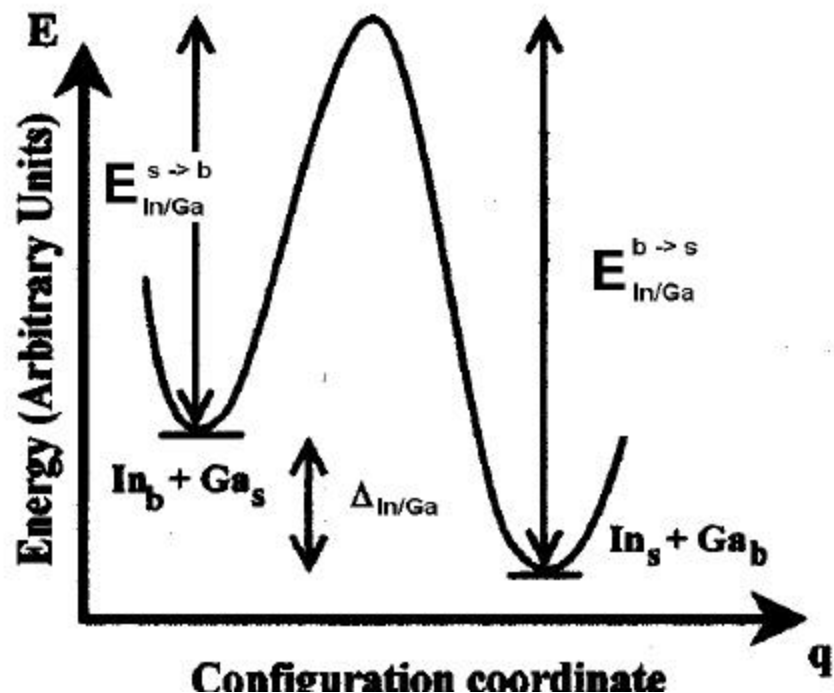
# Model II: The kinetic model of MBE growth



- Cations:  $E_{\text{In/Ga}}^{b \rightarrow s}$  (subsurf In  $\leftrightarrow$  surf Ga)  
 $E_{\text{In/Ga}}^{s \rightarrow b}$  (subsurf Ga  $\leftrightarrow$  surf In)
- Anions:  $E_{\text{Sb/As}}^{b \rightarrow s}$  (subsurf Sb  $\leftrightarrow$  surf As)  
 $E_{\text{Sb/As}}^{s \rightarrow b}$  (subsurf As  $\leftrightarrow$  surf Sb)

Segregation  
Energies:

$$\Delta_{\text{In/Ga}} = E_{\text{In/Ga}}^{s \rightarrow b} - E_{\text{In/Ga}}^{b \rightarrow s}$$



## Model II - The kinetic growth model: the rate equations

- The rates of the exchange reactions depend on the growth temperature  $T_g$

$$P_i = n_i \exp(-E_{A/B}^i / k_B T_g)$$

- The rate of change of the concentration  $x_A(t)$  of surface A atoms is:

$$\frac{dx_A^s(t)}{dt} = \Phi_A(t) + P_{A/B}^{b \rightarrow s} x_A^b(t) x_B^s(t) - P_{A/B}^{s \rightarrow b} x_A^s(t) x_B^b(t)$$

- Under the conditions of the conservation of A atoms, of the total number of atoms and:

$$x_A^b(t) + x_B^b(t) = 1$$

For cations:  $E_{\text{In/Ga}}^{b \rightarrow s} = 1.8 \text{ eV}$ ,  $E_{\text{In/Ga}}^{s \rightarrow b} = 2.0 \text{ eV}$   
(Dehaese et al. APL 66, 52 (95))

**No values in the literature for the anions**

# The barrier energies for anions

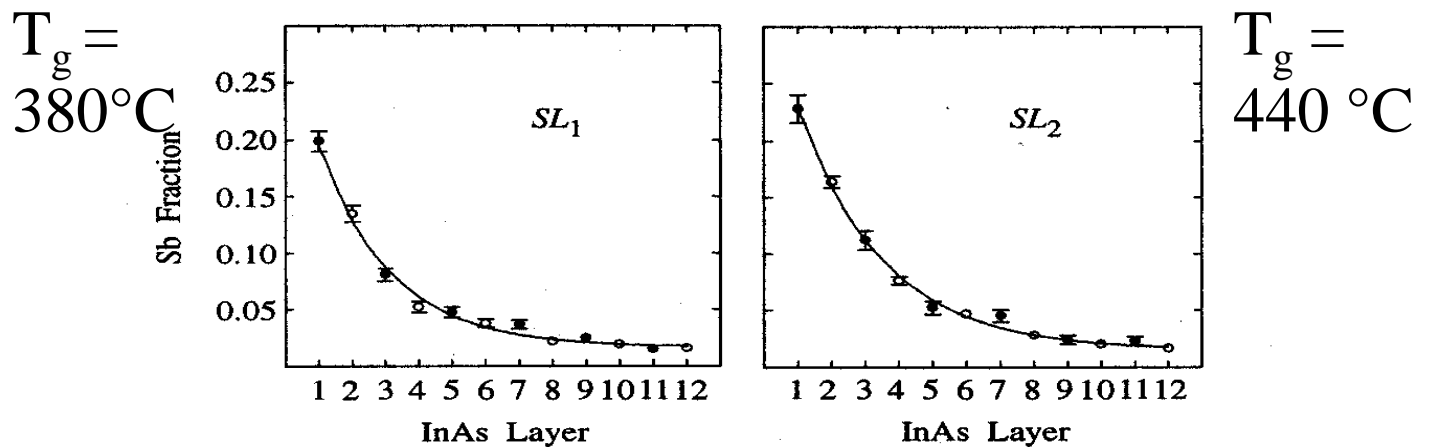
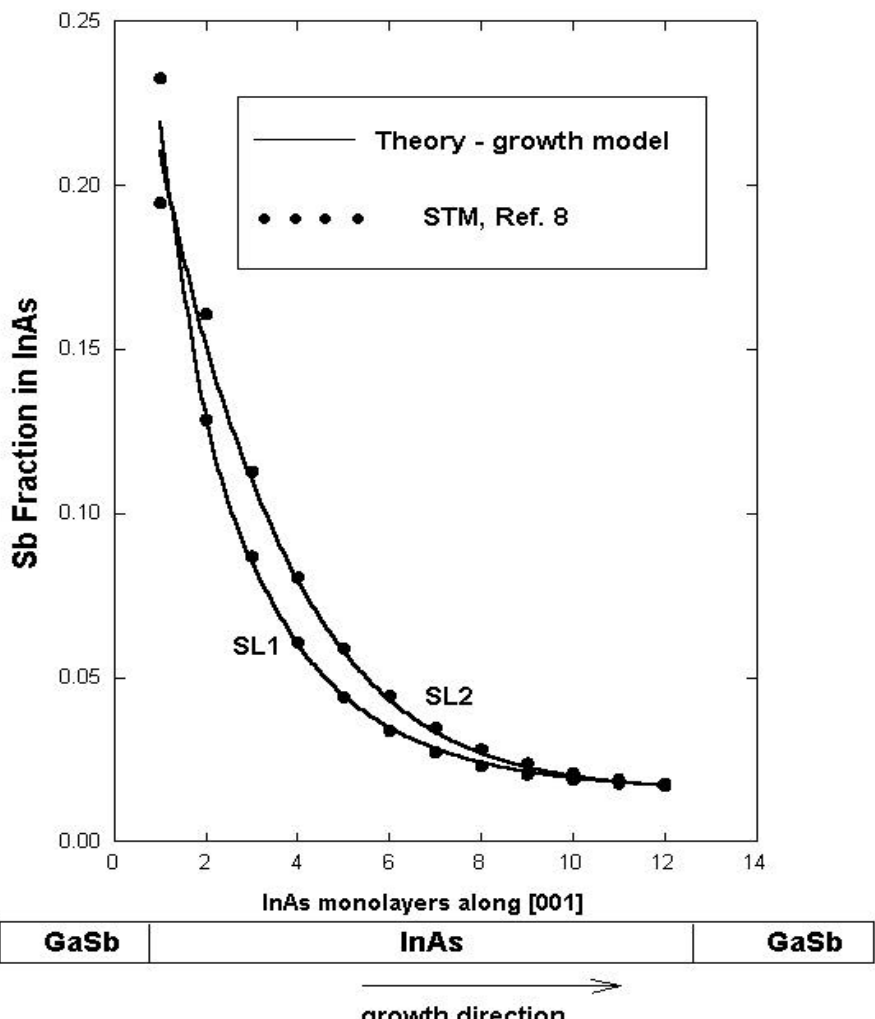


FIG. 4. Segregation profiles constructed from interleaving even (open symbols) and odd (closed symbols) samplings of the As planes in  $SL_1$  (left) and  $SL_2$  (right). Solid lines are fits to Eq. (1).

Steinshnider et al.,  
PRL 85,4562  
(2000)

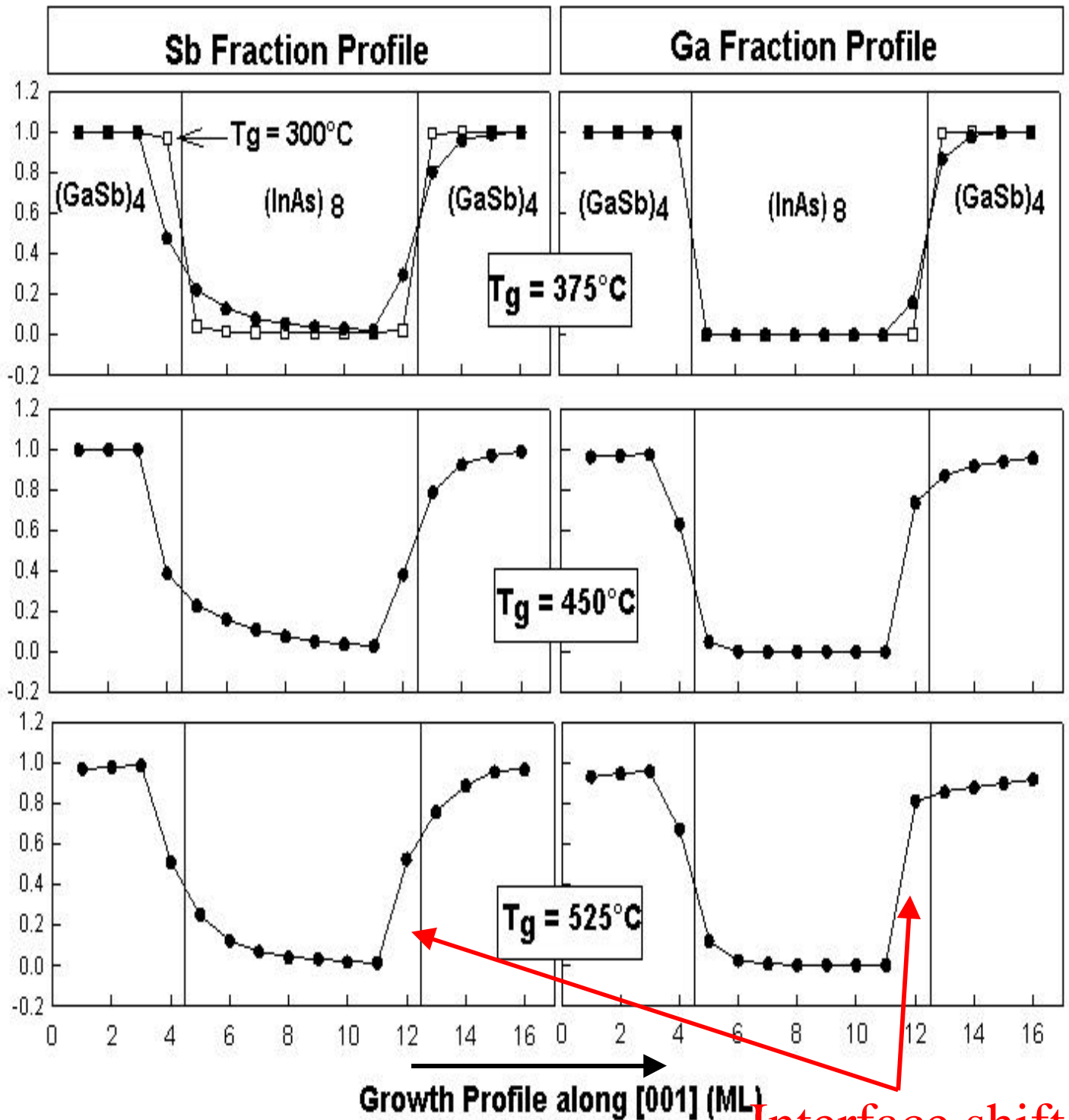
- Fit the growth model to exptl Sb profiles
- $E_{\text{Sb/As}}^{b \rightarrow s} = 1.68$  eV
- $E_{\text{Sb/As}}^{s \rightarrow b} = 1.75$  eV
- $r = 0.25$  ML/s



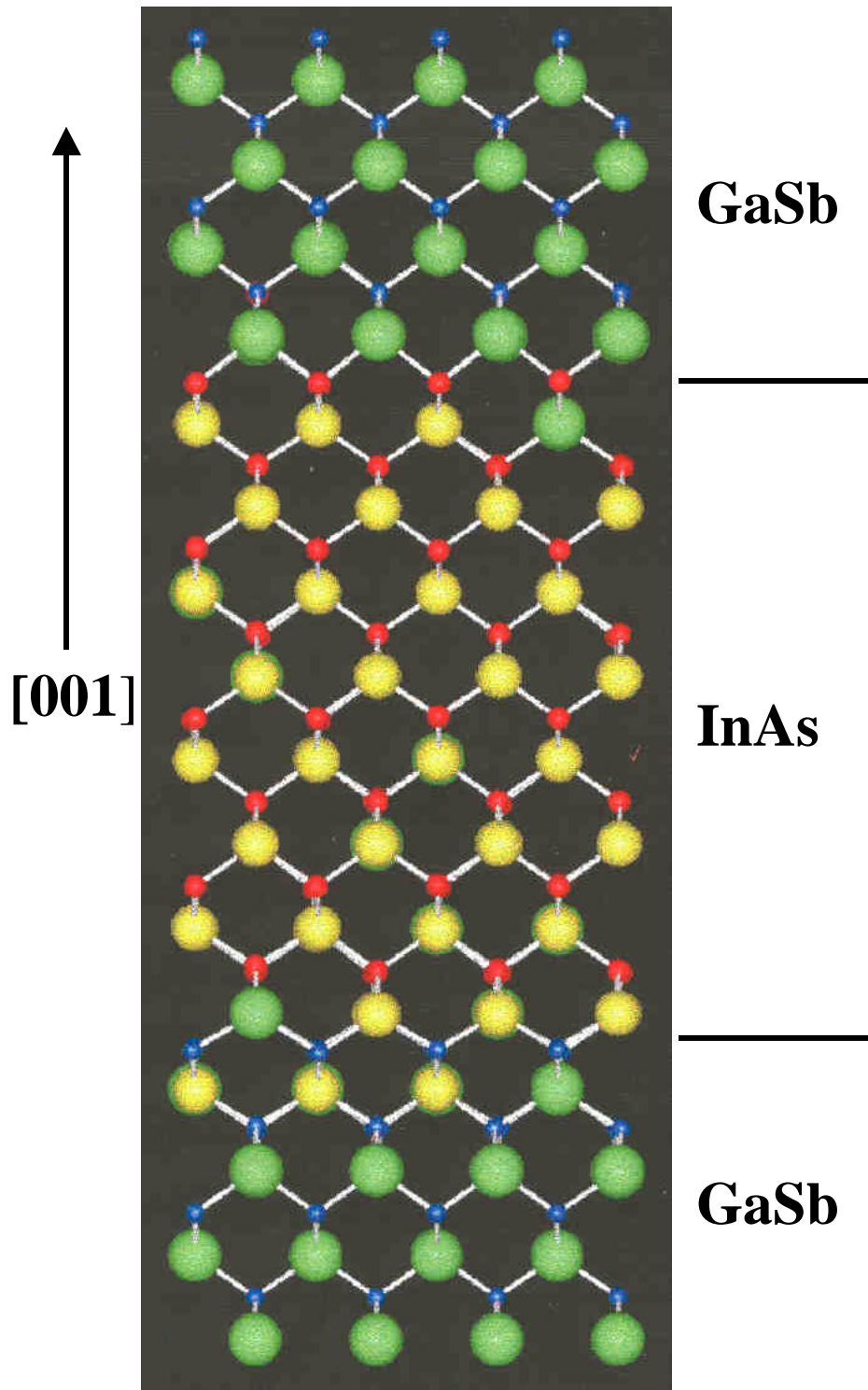
## Model II

# Superlattice segregation profiles

$(\text{InAs})_8/(\text{GaSb})_8$

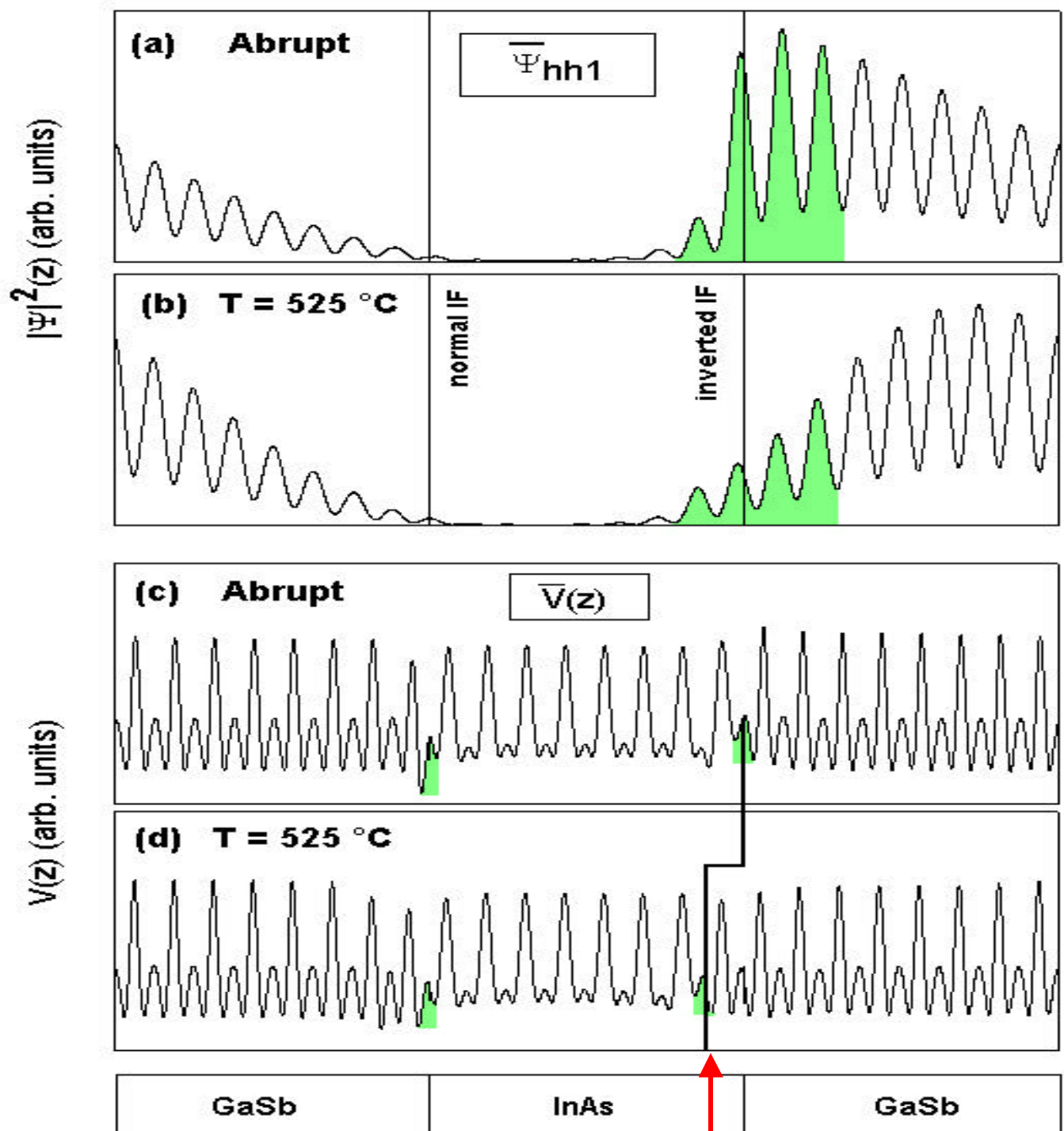


- We assume random atomic arrangements in the (001) planes perpendicular to growth direction consistent with the planar composition profile dictated by the growth model



- Atomic positions in the crystal are locally displaced by a VFF approach

# Modification of the heavy hole localization and of the IF potential with segregation



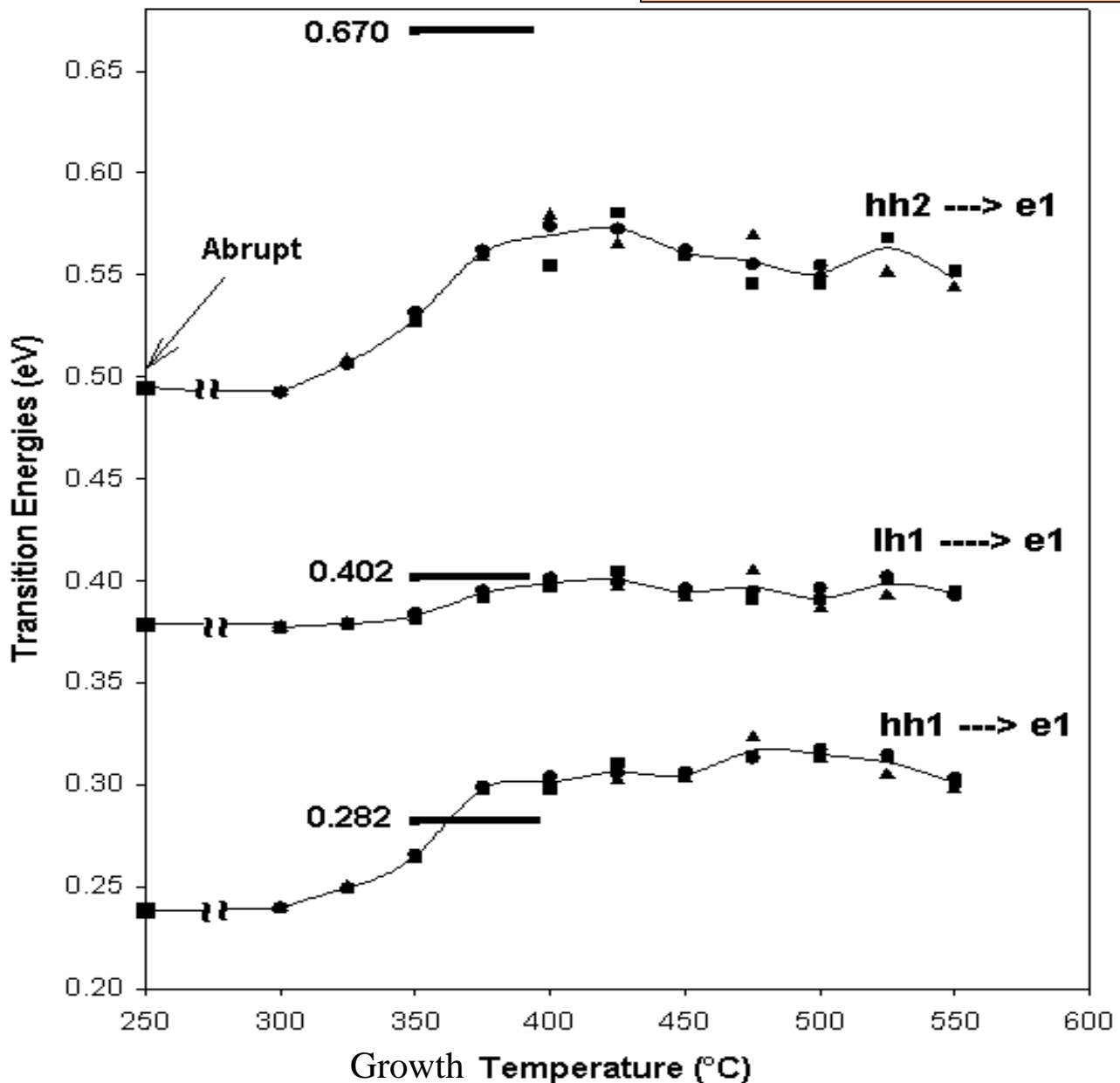
$(\text{InAs})_8/(\text{GaSb})_{16}$

Interface shift

## Model II

# Effects on transition energies

$(\text{InAs})_8/(\text{GaSb})_8$

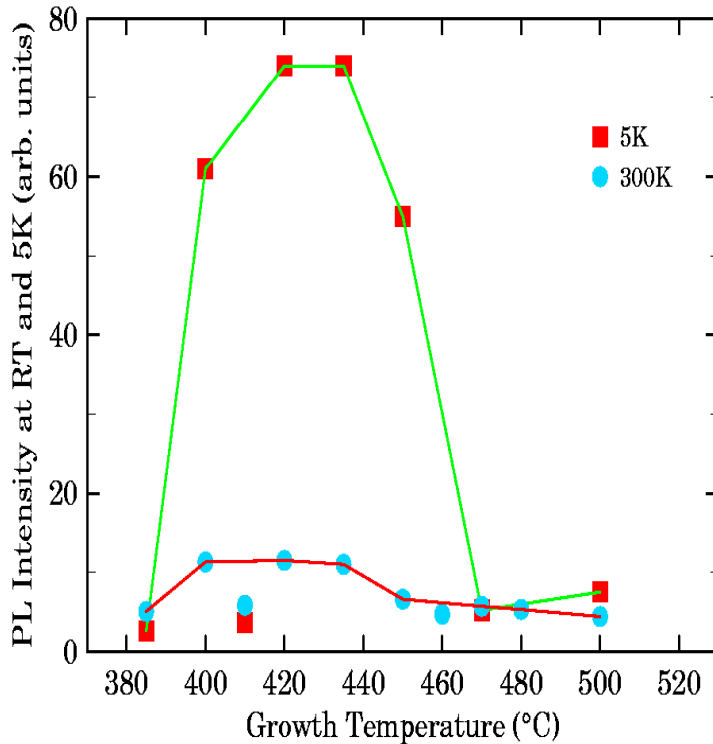


- Large blue shift of heavy hole -  $e_1$  transitions (50 meV for hh1-  $e_1$ )



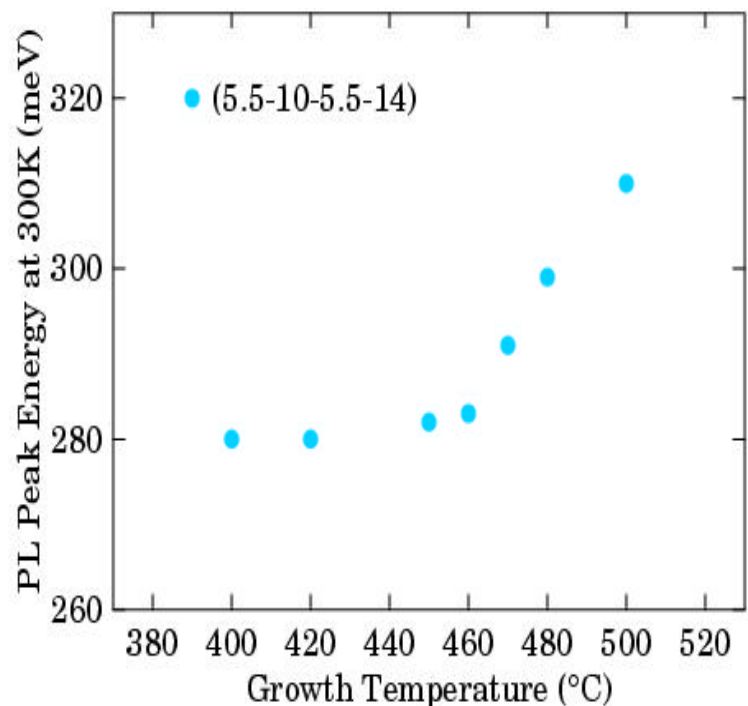
# DEPENDENCE ON GROWTH TEMPERATURE

*M. J. Yang, W. J. Moore, B. R. Bennett, and B. V. Shanabrook,  
Electron. Lett. 34, 270 (1998)*



**PL intensity (laser structures) varies rapidly with growth temperature – Optimal range is 400-450 °C**

**Surprisingly, PL peak (energy gap) also increases significantly with  $T_{\text{growth}}$  above 450 °C!**

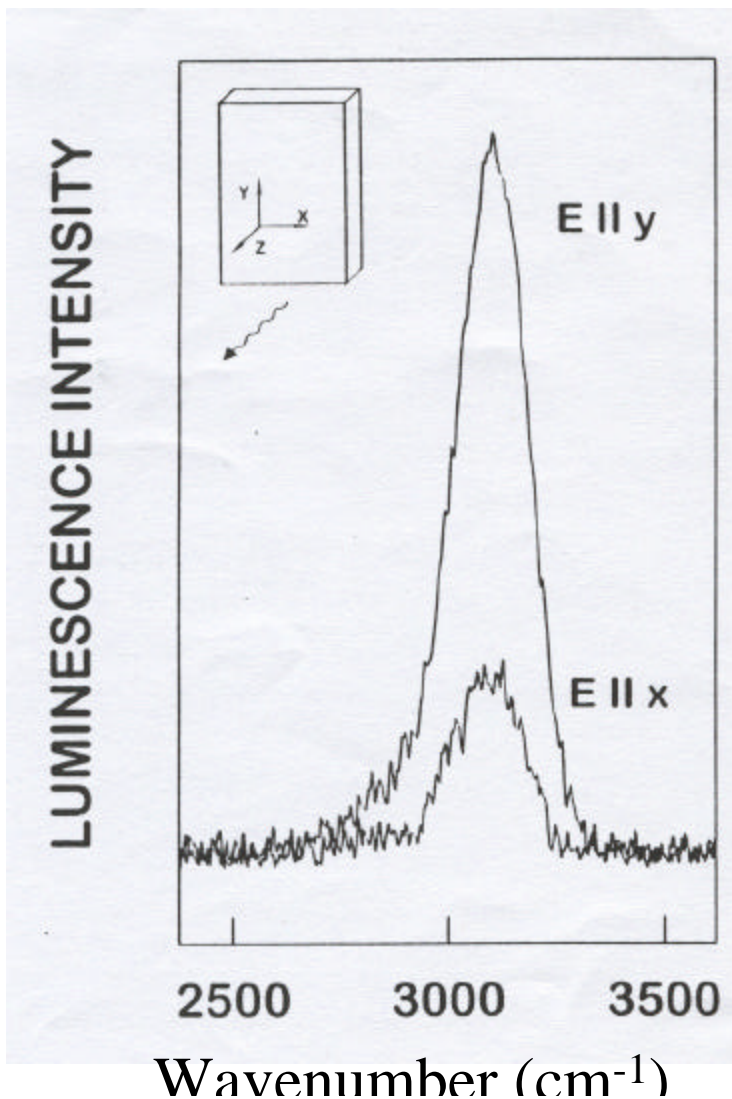




# In-plane Polarization Anisotropy

When symmetry is  $C_{2v}$ :

$$\frac{I^{e \rightarrow h}(\vec{p} \parallel [110])}{I^{e \rightarrow h}(\vec{p} \parallel [\bar{1}10])} \neq 1$$

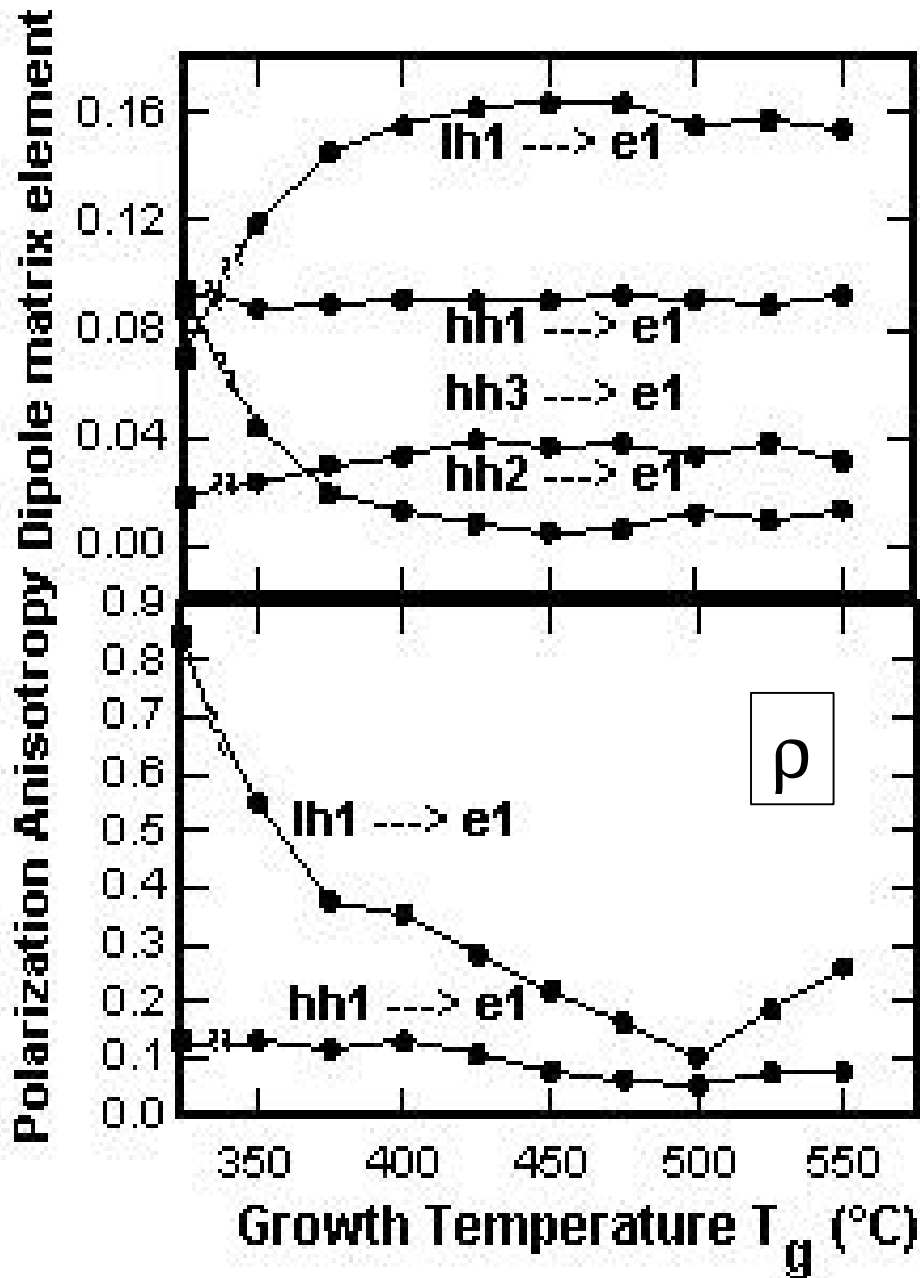
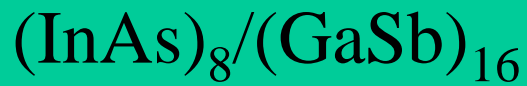


Y=[-110]

X=[110]

InAs/AlSb  
superlattice

Fuchs et al. in  
“Antimonide-Related  
Strained-Layer  
Heterostructures”



$$r = \frac{|P_{110} - P_{-110}|}{[P_{110} + P_{-110}]}$$

- decrease of lh1-hh2 coupling
- decrease of in-plane PA

# Summary

- We have modeled interfacial interdiffusion and disorder to study the effects of:

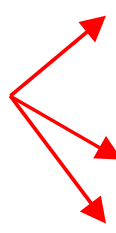
(1) Interfacial Bonds (Model I)

(2) Atomic Segregation (Model II)

## Results

- Band Gaps are **lower** (50 meV for  $n = 8$  SL's) with InSb IFs than with GaAs IFs.
- The **hh1 wavefunction** is strongly **localized** on the In-Sb IF bonds (relative pinning of its energy).
- **Segregation:**

Effects  
increase  
with  $T_g$

- 
- Normal IF: anion intermixing and IF broadening
  - In penetration into GaSb
  - As segregation at the inverted IF

- Segregation causes **blue shifts** of band gaps.
  - • 1 ML narrowing of the InAs well
  - • Reduction of hh1 localization on the InSb IF